

# **UNCERTAINTY OF OPTICAL FLOW: REGRESSION CALIBRATION INSIGHTS**

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## **CONTEXT AND OBJECTIVES**

Reliable optical flow is crucial for many vision tasks related to navigation or planning. Deep neural networks achieve state-of-the-art performance on the problem of optical flow estimation. We would like to have a tool to indicate the reliability of optical flow which is the uncertainty estimator for optical flow.

- In this work we aim to quantify epistemic uncertainty for optical flow by using existing approaches.
- We use two different evaluation tools to measure the performance of uncertainty estimators, one is for the uncertainty ordering, one is for regression calibration degree.



• Our work gives insights on optical flow uncertainty calibration problem Fig. 1: Demonstration of optical flow prediction and one of its uncertainty estimation. We use FlowNetS and the trade-offs which occur depending on the considered uncertainty [Dos+15] trained on the FlyingChairs [Dos+15] dataset and tested on KITTI [MG15] training set. The estimation frameworks. uncertainty map is made by MC Dropout [GG16] as an example.

### **DEEP NEURAL NETWORK AND UNCERTAINTY ESTIMATION**

- MC Dropout [GG16]: aim to find the posterior distribution of the parameters given the training dataset  $P(\Theta \mid D)$ , not only the values corresponding to the MAP. To make a prediction y on a new sample x the BNN compute :  $P(y \mid x, D) = \int P(y \mid x, \Theta) P(\Theta \mid D) d\Theta$ . We set Dropout layers in the model and do multiple forward propagations and calculate the variance among the inferences.
- Deep Ensembles[LPB17]: Train multiple deep neural networks to have access to their uncertainty. Each of the networks optimizes a heteroscedastic uncertainty loss [KG17] which considers that the output of optical flow model is a Gaussian distribution, the mean is the flow prediction and the variance is the uncertainty. Finally we combine the variances to get the final uncertainty.
- Kullback-Leibler divergence: The ground-truth that we want to match is a Gaussian distribution of mean the optical flow and of variance the square error of the optical flow. This loss aims to see if KL is more suitable than the previous heteroscedastic loss used in deep ensembles.
- L2 regression: a simple strategy using regression with means squared error loss. The trained variance is targeting the square error of the flow prediction.

#### **UNCERTAINTY EVALUATION METHODS**

- **Sparsification Curve** [Ilg+18]: is a kind of Accuracy-Rejection Curve. It is a relative quality indicator: it reports the correctness of relative uncertainty ordering of the observed pixels with respect to the ideal ordering.
- Calibration Curve[KFE18]: has not yet been employed for optical flow analysis, is an absolute quality indicator, and it underlines the correlation between the expected confidence level taking into account the groundtruth and the confidence level reported by the variance estimator. The

### **SEQUENTIAL TRAINING FOR UNCERTAINTY**



uncertainty estimation should be wider enough to cover the error zone confidently but also as sharp as possible.

Fig. 2: We use a pre-trained and frozen optical flow model to make flow estimations and feed them to the loss to train the uncertainty estimator. Solid line: forward propagate; Dotted line: backward propagate; Black line: Procedure only during training; Green line: Procedure during inferring and training.

#### **EXPERIMENTAL RESULTS**

We train a FlowNetS [Dos+15] on FlyingChairs [Dos+15] for its flow and uncertainty predictions in combining with different uncertainty estimation approaches (MC: MC) Dropout; L2: L2 regression targeting square error; KL: KL-divergence;  $EDE_i / PDE_i$ : empirical/predictive deep ensembles with i samples) by using sequential training. Then we evaluate the performance of different approaches on KITTI[MG15] without fine-tuning on it.

Curve Type	Calibration Error				Sparsification Error				Run
Noise Type	Gaussian Noise		Motion Blur		Gaussian Noise		Motion Blur		time
Method Name	AUC	RC	AUC	RC	AUC	RC	AUC	RC	(ms)
MC	1.0191	0.0171	0.9763	0.0206	0.5102	0.0406	0.4232	0.0137	196
L2	0.8158	0.0059	0.8241	0.0122	1.5801	0.2759	1.7393	0.3513	32
KL	1.0139	0.0148	1.0139	0.0327	0.9577	0.0398	0.8051	0.0696	32
$PDE_1$	0.9719	0.0111	0.9559	0.0150	1.4238	0.0536	1.2272	0.0366	32
$EDE_2$	1.0604	0.0192	0.9689	0.0264	1.0397	0.1044	1.1384	0.1331	69
$PDE_2$	0.9704	0.0209	0.9182	0.0189	0.8721	0.0512	0.8432	0.0438	66
$EDE_3$	1.0330	0.0128	0.9520	0.0304	0.7112	0.0868	0.7016	0.0815	99
$PDE_3$	0.9529	0.0143	0.9146	0.0146	0.7763	0.0465	0.7001	0.0183	101
$EDE_4$	1.0133	0.0126	0.9262	0.0265	0.6370	0.0751	0.5860	0.0598	131
$PDE_4$	0.9449	0.0117	0.8985	0.0185	0.7264	0.0431	0.6370	0.0216	136
$EDE_5$	1.0297	0.0153	0.9357	0.0297	0.8901	0.1549	0.7961	0.1343	165
$PDE_5$	0.9691	0.0157	0.9106	0.0150	0.8826	0.1021	0.8241	0.0894	172

**Table. 1:** Area under the curve (AUC) and rate of change of the curve (RC) for the calibration error **Fig. 3:** Uncertainty visualizations for different estimation methods. To visualize the uncertainties we combine distribution ensembles; Bold values: the best ones; Red values: the worst ones. Run time: time consumption for outputting mean and variance, the test is executed on 1 NVIDIA TITAN RTX.



the variance from two channels based on our hypothesis, and we use the entropy of a Gaussian distribution. For the joint visualization, all entropies are re-scaled using the maximum value among them.

#### CONCLUSIONS

- In-depth characterization of current most popular techniques for uncertainty estimation applied to optical flow.
- Proposal of a new plug-in training technique, loss and criteria.
- Support for transferring a model trained on synthetic data and applied in real-world, diverse settings.

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